

## Exercise 12

Let  $a_0, a_1, a_2, \dots, a_n$  ( $n \geq 1$ ) denote *real* numbers, and let  $z$  be any complex number. With the aid of the results in Exercise 11, show that

$$\overline{a_0 + a_1z + a_2z^2 + \cdots + a_nz^n} = a_0 + a_1\bar{z} + a_2\bar{z}^2 + \cdots + a_n\bar{z}^n.$$

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### Solution

$$\begin{aligned}\overline{a_0 + a_1z + a_2z^2 + \cdots + a_nz^n} &= \bar{a}_0 + \bar{a}_1\bar{z} + \bar{a}_2\bar{z}^2 + \cdots + \bar{a}_n\bar{z}^n \\ &= a_0 + a_1\bar{z} + a_2\bar{z}^2 + \cdots + a_n\bar{z}^n \\ &= a_0 + a_1\bar{z} + a_2\bar{z}^2 + \cdots + a_n\bar{z}^n\end{aligned}$$